

A methodology for population estimation at the national and provincial levels: The approach used by Statistics South Africa

1. Overview

In order to meet the need for population estimates, Statistics South Africa publishes national and provincial population estimates annually. This paper provides users of the mid-year population estimates with a detailed description of the methodology employed by Statistics South Africa. The actual estimates may be downloaded from the Statistics South Africa website.

We distinguish between three phases in our projections. These are:

- (a) Application of the Estimation and Projection Package (EPP) to obtain an HIV epidemic curve;
- (b) Projection of the national population by using the SPECTRUM system;
- (c) Provincial projection by applying a UN sub-national method of cohort-component projections (United Nations, 1992). The software for these projections was written in JMP script language (JSL) developed by the SAS institute Inc.

For each mid-year estimate, a new set of projections are prepared with 2001 as the base year. Based on new birth and death information, new fertility and mortality assumptions are made. Adjustments in this regard are also made from 2001. New versions of the SPECTRUM program incorporate new survey results on HIV/AIDS and the effect on mortality and fertility levels.

Stats SA releases the mid-year estimates every year in July on its website (www.statssa.gov.za). These estimates are unique for each year due to the assumptions that are made and the data inputs. It is therefore important to note that population and other demographic data in each release form a new set of time series. Users should therefore compare the time series data in each statistical release and not data between statistical releases.

2. National projections

2.1 Models for projection

Demographic-based programmes that incorporate an epidemiological component were developed by different organisations. Four of the most important models from a South African viewpoint are: (a) the Spectrum Modeling System developed by the Futures Group; (b) the RupHivAids model developed by the US Census Bureau; (c) the abcDIM model which is developed and used by the United Nations Population Division (UNPD) and; (d) the ASSA model developed by the Actuarial Society of Southern Africa.

When Stats SA started its new round of population projections in 2003, the documentation of the RupHivAids model was not completed (and will probably not be developed further) and the abcDIM software was at that stage an in-house programme that was used to do population projections of all the countries in the world. The choice was therefore between ASSA and Spectrum and Stats SA decided to follow the Spectrum route.

The Spectrum Policy Modeling System (Futures Group) consists of 7 components, but Stats SA used only two of them in this projection, namely (a) **Demproj** for population projections and (b) **AIM** in which the consequences of the AIDS epidemic were projected.

The population projections, which apply the cohort-component method, must first be prepared before AIM can be used. In this projection with base-year 1985, fertility, mortality and international migration for the projection period are required. Life Expectancies and Total Fertility rates without taking AIDS into account were used as inputs in the model.

The base year populations and projected populations on the 1996 and 2001 census dates are given in Table 1 below. It can be seen from this table that according to the Stats SA projections the estimated 1996 population figure was 0,83 million higher than the published 1996 Census, while a difference of just over 20 thousand can be found between the published 2001 Census and this projection on that date. Greater differences were however found regarding the sex-ratios and age-distributions (not shown here).

Table 1: Base and projected South African populations

	Base (1985) mid-year population	Reported 1996 Census	Stats SA projection on 1996 Census date	Reported 2001 Census	Stats SA projection on 2001 Census date
African	23,68	31,13	31,45	35,42	34,93
Coloured	3,02	3,60	3,71	4,00	4,00
Asian	0,88	1,05	1,06	1,12	1,13
White	4,74	4,43	4,82	4,29	4,75
Total	32,32	40,21	41,04	44,83	44,81

2.2 Adjustment of Antenatal Clinics (ANC) data and HIV Prevalence estimates

The USAID|Health Policy Initiative (HPI) and its predecessor projects have developed computer models that analyse existing information to determine the future consequences of today's development programmes and policies. The Spectrum Policy Modeling System consolidates previous models into an integrated package containing seven components. Stats SA only uses two of these components to project the South African populations on national level. These components are **Demproj**, a programme to make population projections using the cohort component method and **AIM**, a programme to project the consequences of the AIDS epidemic. The mid-year population estimates in this report were obtained by using Spectrum version 4.392.

An important input in **AIM** is the HIV prevalence of the South African population and we will now explain why Stats SA decided on certain levels.

Our knowledge of the HIV epidemic in South Africa is based primarily on the prevalence data that have been collected annually from pregnant women attending public antenatal clinics (ANC) since 1990. These data have been used to obtain national estimates of HIV prevalence among the adult population and to determine epidemic trends over time.

To obtain a national epidemic curve, the Estimation and Projection Package (EPP) which now has been incorporated into SPECTRUM (Version 4.392) were applied using HIV prevalence data for the period 1990–2009 obtained from pregnant women attending antenatal clinics in South Africa.

ANC data however produce biased estimates of general population HIV prevalence because only a select group of people (i.e., pregnant women attending public health services) are included in the sample. Firstly, HIV prevalence among women who attend public health

services is generally estimated to be higher than prevalence among those who attend private health services. Secondly, HIV prevalence among pregnant women is likely to be different than the prevalence among the general adult population. In order to correct for these biases we adjusted the ANC prevalence estimates by adjusting for relative attendance rates at antenatal clinics and by adjusting for the difference in prevalence between pregnant women and the general adult population.

Ideally, national HIV prevalence surveys would be an unbiased sample of the general adult population if the response rate is high, but with the 2008 HSRC population-based survey the overall response rate for adults aged 15–49 years was 67,6% (HSRC, 2009). If non-responders are more likely to be HIV positive than responders, then the HSRC survey is likely to underestimate the true HIV prevalence.

2.2.1 Correction factors applied to ANC data

Adjusting for relative attendance rates at antenatal clinics

This adjustment requires that the ANC data be standardised for race because the race distribution of ANC attendees is different from the distribution in the general population. This standardisation was based on the ANC prevalence of HIV by race and on the race distribution of the adult population in South Africa. Ideally, the standardisation should be based on the distribution of pregnant women but since this was not available we used the race distribution for the adult population (age 15–49 years) as per the latest available population estimates from Statistics South Africa (Statistics South Africa, 2009). Data on proportional attendance rates were obtained from the Department of Health. The correction factor was then calculated as the ratio of the unadjusted prevalence to the race-standardised prevalence. Because of differences in ANC attendance and race distribution between provinces the correction factor was calculated for each province.

Adjusting for prevalence in pregnant women versus prevalence among adults

This correction factor relates to the use of prevalence among pregnant women to estimate prevalence among the general adult (men and women) population. The 2008 national HSRC survey in South Africa showed that prevalence among pregnant women was 22,6%, while in the general population it was 16,9% among men and women (aged 15–49 years) combined (HSRC, 2008).

To adjust for the difference between HIV prevalence in pregnant women and prevalence among adults in the general population, a correction factor based on the ratio of prevalence in these two groups was calculated using the data from the HSRC, i.e., $16,9/22,6 = 0,75$. In the absence of prevalence data for pregnant women by province, we assumed that this ratio is similar for all provinces.

Combined adjustment

The combined correction factor was finally calculated for each province as the product of the two correction factors described above and was applied to provincial ANC HIV prevalence estimates to obtain the adjusted prevalence estimates. The national adjusted prevalence was then obtained from the provincial estimates.

The following correction factors were applied to the ANC provincial estimates prevalence estimates (see Table 2).

Table 2: Projection factors applied to ANC provincial prevalence estimates

Province	Correction factor	Adjusted 2008 ANC prevalence
Eastern Cape	0,71	18,8
Free State	0,65	21,4
Gauteng	0,68	20,3
KwaZulu-Natal	0,64	24,8
Limpopo	0,75	15,5
Mpumalanga	0,72	25,6
Northern Cape	0,68	11,0
North West	0,70	21,7
Western Cape	0,55	8,9

A national epidemic curve was obtained in EPP from the adjusted provincial prevalence data. These estimates were used as input in the Spectrum projection (version 4.392) software.

3. Provincial projections

3.1 Overview

When projections for all the regions of a country are desired and the appropriate data are available, a multi-regional approach should be considered, as this is the only way to

guarantee that the total migration flows between regions will sum to zero, or to the assumed level of international migration (United Nations, 1992). Developed by Willekens and Rogers (1978), these methods have not been widely used in developing countries, largely due to the lack of adequate migration data and the difficulty of applying these methods.

Multi-regional methods require the estimation of separate age-specific migration rates between every region of the country and every other region, and such detailed data are rarely available. Although it is possible to estimate some of the missing data (see Willekens *et al.*, 1979), the task of preparing data can become overwhelming if there are many regions. If there are only a few streams, however, the multi-regional method is the best method to use. In South Africa, 2448 (9x8x17x2) migration streams are derived if the multi-regional model is applied in calculating migration streams by age group (17 in total) and sex for each province. The number of streams increase dramatically if this approach is followed for the 52 district councils/metros, namely to about 90 000.

3.2 The age-structure of the provinces

The base from which a population projection is done is very important as it has a big effect on the outcome of a projection. It also forms the base from which the provincial fertility and mortality rates were adjusted in this study.

For the preparation of the 2001 age-structures of the provinces, three sources of data were used, namely (a) the provincial 2001 Census populations by age and sex; (b) the projected South African population by age and sex; and (c) independent estimates of the provincial totals by sex.

In this projection the independent estimates were obtained by applying estimated birth, death and net migration data for the period 1996 to 2001 (from Census 2001) to the adjusted 1996 Census totals. This analysis provides a first estimate of the relative size of the provinces and was done separately for males and females.

Using the three sources of data mentioned above, the 2001 base age structures of each of the nine provinces by sex is determined by applying an iteration process. Five iterations were enough to obtain stable populations.

3.3 Calculation of migration rates from the 2001 Census and 2007 Community Survey (CS) of Stats SA

For sub-national areas, migration is often the major determinant of population growth and can also be seen as the most difficult component of growth to forecast accurately as they are subject to much greater volatility than either fertility or mortality rates.

To determine flow patterns a census or large survey is usually the only source of data and the two procedures most frequently used for measuring internal migration are:

- (a) Procedures based on questions on censuses or surveys intended to detect migration.
- (b) Procedures based on other population characteristics such as age-structure and places of birth.

As special questions in Census 2001 and in CS 2007 were available, it was decided to follow the approach in (a) above, in the Stats SA study. These questions were used to determine the usual residence and previous residence of every person during the the census or survey period. In the case of the census the targeted previous residence was exactly five years, while the CS referred to the period October 2001 to February 2007.

To convert the response to these migration questions to migration rates per thousand of the population in specific age groups, the following steps were followed:

- (a) Determine the usual province of residence of each person at the time of the census or survey.
- (b) Determine the previous province of residence.
- (c) If the usual province of residence and the previous province of residence were the same, then the person is classified as a non-migrant.
- (d) If the usual province and previous province are different the direction of the migration stream is determined.
- (e) Cross tabulate usual and previous province (see Table 3 below).
- (f) Cross tabulate age (five-year age groups) with usual province for every previous province (see Table 4).

We are now ready to convert the migration information obtained from Census 2001 and/or CS 2007 to migration rates per thousand of the population. This is done by using two sets of information, namely the cross-tabulations of previous and usual provinces for the total population and by age groups. Table 3 below is used to determine the level of migration

movements between the provinces. To illustrate the procedure, only the female movements from Census 2001 are given in this table.

From Table 3 it is observed that for example 94,12 % of the population of the Eastern Cape reported that they were living in the same province in 1996 and 2001. This however did not indicate that they did not move as the census question did not focus on the last move. Of those that moved 2,4 % moved to Western Cape, 1,5 % to Gauteng and smaller proportions to other provinces.

Table 3: Total female movement between provinces: 1996-2001 (percentages)

Prov In 1996	Province in 2001								
	EC	FS	GT	KZN	LIM	MP	NC	NW	WC
EC	94,12	0,2748335*	1,50	1,00	0,11	0,16	0,06	0,40	2,38
FS	0,32	95,04	2,53	0,33	0,18	0,25	0,25	0,77	0,50
GT	0,34	0,30	96,57	0,54	0,49	0,41	0,08	0,55	0,72
KZN	0,22	0,10	1,47	97,55	0,08	0,21	0,02	0,09	0,27
LIM	0,06	0,08	3,48	0,10	95,21	0,62	0,03	0,31	0,10
MP	0,12	0,19	2,88	0,37	0,63	95,32	0,05	0,26	0,20
NC	0,33	0,87	1,39	0,22	0,20	0,15	93,36	1,01	2,46
NW	0,18	0,36	3,53	0,16	0,41	0,19	0,44	94,49	0,26
WC	0,69	0,13	0,84	0,24	0,07	0,08	0,27	0,09	97,58

* This FS cell has more decimal places in order to illustrate the calculations in Table 9.

The next step is now to determine the age distribution of the out-migrants from each province to every other province. The results of these analyses are given in Table 4 to illustrate the out-migration of the female Eastern Cape population to the other eight provinces. To complete the analyses eight similar tables (not shown here) have been constructed.

Table 4 does not show the volume of migration, but only indicates the age distribution of the migrants. It is clear from this table that the highest percentage of migrants are found amongst those in the age group 15–24. For example in Gauteng about 45% of the out-migrants were from the age group 15–24 years.

It is therefore clear that the information in both Tables 3 and 4 must be used to calculate out-migration rates per thousand of the population. An example of such a calculation is given in

Table 5. In this calculation it is assumed that the rates for the period 1996–2001 can be used in the period 2001–2006.

Table 4: Female migrants from Eastern Cape to other provinces (percentage distribution)

Age group	Province in 2001							
	FS*	GT	KZN	LIM	MP	NC	NW	WC
Births after 2001	0,060519991	0,0557	0,0626	0,0747	0,0820	0,0706	0,0810	0,0567
0-4	0,078544898	0,0524	0,0635	0,0836	0,0676	0,0879	0,0650	0,0638
5-9	0,075486126	0,0483	0,0628	0,0494	0,0646	0,0855	0,0406	0,0652
10-14	0,120166048	0,1073	0,1291	0,0922	0,1145	0,1257	0,0814	0,1325
15-19	0,187786760	0,2446	0,2402	0,1598	0,1768	0,1299	0,1979	0,2448
20-24	0,151846187	0,2126	0,1682	0,1638	0,1745	0,1327	0,2059	0,1823
25-29	0,107712475	0,0982	0,0881	0,1355	0,1168	0,0850	0,1320	0,0867
30-34	0,071444177	0,0638	0,0612	0,0857	0,0768	0,0729	0,0882	0,0543
35-39	0,049705047	0,0436	0,0428	0,0593	0,0462	0,0579	0,0531	0,0381
40-44	0,029495303	0,0266	0,0261	0,0379	0,0233	0,0519	0,0252	0,0241
45-49	0,019008084	0,0151	0,0176	0,0198	0,0157	0,0276	0,0102	0,0154
50-54	0,011361154	0,0095	0,0112	0,0097	0,0094	0,0257	0,0066	0,0110
55-59	0,011033428	0,0075	0,0095	0,0097	0,0105	0,0140	0,0047	0,0091
60-64	0,008302381	0,0051	0,0057	0,0044	0,0073	0,0084	0,0025	0,0060
65-69	0,006663754	0,0033	0,0055	0,0052	0,0050	0,0098	0,0022	0,0043
70-74	0,005571335	0,0031	0,0025	0,0044	0,0046	0,0065	0,0018	0,0025
75-79	0,003604981	0,0019	0,0020	0,0026	0,0029	0,0042	0,0008	0,0018
80+	0,001747870	0,0013	0,0013	0,0024	0,0017	0,0037	0,0010	0,0013
Total	1	1	1	1	1	1	1	1

* The FS column has more decimal places in order to illustrate the calculations in Table 9.

Table 5: Calculation of "scaled" migration rates (out-migration of Eastern Cape females to the Free State in the period 2001 to 2006)

Age in 2001	EC Female Population in 2001	Out migration rates from the EC to the FS (Table 4)	Estimated migrants	Scaled migration rates
Births after 2001		0,060519991		0,001936
0-4	387 164	0,078544898	30 410	0,002513
5-9	446 561	0,075486126	33 709	0,002415
10-14	450 993	0,120166048	54 194	0,003844
15-19	403 541	0,187786760	75 780	0,006007
20-24	305 412	0,151846187	46 376	0,004858
25-29	253 482	0,107712475	27 303	0,003446
30-34	199 671	0,071444177	14 265	0,002285
35-39	182 789	0,049705047	9 086	0,001590
40-44	182 212	0,029495303	5 374	0,000944
45-49	153 021	0,019008084	2 909	0,000608
50-54	127 907	0,011361154	1 453	0,000363
55-59	108 174	0,011033428	1 194	0,000353
60-64	119 473	0,008302381	992	0,000266
65-69	91 015	0,006663754	607	0,000213
70-74	61 401	0,005571335	342	0,000178
75-79	35 740	0,003604981	129	0,000115
80+	31 958	0,001747870	56	0,000056
Total	3 540 514	1	304 177	
Calculated total out-migration rate			$304\,177 / 3\,540\,514 = 0,0859132$	
Desired total out-migration rate (from Table 3)			0,002748335	
Scale factor			$0,002748335 / 0,0859132 = 0,03198967$	

The scaled migration rates in the last column of Table 5, was calculated by applying the scale factor to the census migration rates (third column). These out-migration rates for the Eastern Cape females to the Free State will be used in the cohort-component projections. For each of the nine provinces, sixteen tables of the format of Table 5 are created.

3.4 Provincial fertility rates

The following steps were used to obtain a set of age-specific fertility rates for each province to be used in the provincial cohort-component projections:

- (a) For each province a preliminary set of age-specific fertility rates were obtained. In this analysis the rates were taken from a report by Moultrie and Dorington (2004) and fertility information from CS 2007.
- (b) Analyses of the recorded birth datasets (for the period 1998 to 2008) were also done to place the results obtained from (a) into perspective.
- (c) The preliminary age-specific fertility rates were then applied to the female population aged 15 to 49 years to calculate the number of births. This was done for each province.
- (d) The total number of births generated from the provinces were then compared with the total number of births in the RSA projection (phase one). Proportional adjustments were made if necessary and adjusted TFRs calculated.
- (e) Using these adjusted TFRs and age specific fertility rates as well as survival ratios, the number of births and the 0–4 projected population were obtained. The projected 0–4 year and 5–9 year populations were checked for consistency. Provision was made to adjust the TFR manually if inconsistencies were found.
- (f) The process (a) to (d) above was repeated if inconsistencies were found in (e).

3.5 Provincial survival ratios

The following steps were used to obtain a set of survival ratios for each province to be used in the provincial cohort-component projections:

- (a) For each province a preliminary set of life expectancies at birth for males and females were obtained by applying the LTWST spreadsheet in PAS. The calculations were done with the following as input (i) crude death rates (from Census 2001 and the 2007 Community Survey) and (ii) age structures for males and females.
- (b) Analyses of the causes of death datasets from 1998 to 2007 (the latest available) were done to place the results in (a) into perspective.
- (c) Separate Life Tables for males and females and for each province were then constructed from these preliminary set of life expectancies at birth (Far-East pattern of the UN used).
- (d) By using the $m(x)$ -values (age-specific mortality rates) in these life tables, the number of deaths by age can then be calculated for both males and females in each province.
- (e) The numbers of male and female deaths calculated for each province were then compared with the total number of male and female deaths in the RSA projection respectively. Proportional adjustments were made if necessary.

- (f) The adjusted $m(x)$ values were then used to construct life tables. Life expectancies at birth as well as survival ratios by age can be read from the obtained life tables.

An example of the calculations for the female population follows the steps as described above and is given in Table 6. The first step in (a) above is to make assumptions about a preliminary set of life expectancies as described above. In Table 6 below, these values are indicated as shaded areas in column 4. The second step (b) above is to use these life expectancies to create life tables. This was done by using the MATCH application in Mortpak4 and the $m(x)$ -value from the life tables given in column 4 of Table 6. Applying the derived $m(x)$ -values to the population figures will result in the number of deaths per age group. In Table 6 these calculations were done for every province and according to step (d) above, the total number of deaths for all the provinces are compared with RSA number of deaths. In this example the total number of RSA deaths was 294 666 and the deaths by province total 333 314. The adjusted deaths (for each age group in a province) are calculated by applying an adjustment factor of 0,884049274 (294 666 divided by 333 314). The adjusted deaths are given in column 6 in the table below. The last step is to use the adjusted $m(x)$ -values (shaded values in column 7) to construct life tables. This is done by applying the LTMXQXAD spreadsheet in PAS. The survival ratios read from the constructed life tables and which will be used in the projection, are given in the last column of Table 6.

Table 6: Calculation of female survival ratios for provincial projections

	Age category	Population in 2001	Derived $m(x)$ values	Deaths	Adjusted		Survival ratios	
					Deaths	$m(x)$	Categories	Values
EC	0	69 939	0,084125316	5884	5 202	0,0744	Birth	0,9177
	1-4	317 225	0,009896939	3140	2 776	0,0088	0- 4	0,9745

	80-84	21 446	0,154634765	3316	2 932	0,1367	75-79	0,5717
	85+	10 512	0,236319752	2484	2 196	0,2089	80+	0,3913
	EC Total		LE=53,6	52111	46 069	LE=56,3		
FS	0	31 344	0,094427415	2960	2 617	0,0835	Birth	0,9068
	1-4	122 286	0,012152275	1486	1 314	0,0107	0- 4	0,9688

	80-84	7 209	0,161594571	1165	1 030	0,1429	75-79	0,5549
	85+	4 782	0,242804251	1161	1 026	0,2146	80+	0,3794
	FS Total		LE=50,7	23263	20 565	LE=53,6		
GT	0	85 909	0,076565555	6578	5 815	0,0677	Birth	0,9256
	1-4	318 539	0,008381398	2670	2 360	0,0074	0- 4	0,9783

	80-84	15 073	0,149157647	2248	1 987	0,1319	75-79	0,5851
	85+	9 722	0,231211611	2248	1 987	0,2044	80+	0,4008
	GT Total		LE=55,8	51045	45 127	LE=58,4		

Table 6: Calculation of female survival ratios for provincial projections (continued)

KZN	0	110 491	0,114533793	12655	11 188	0,1013	Birth	0,8851
	1-4	464 769	0,017124547	7959	7 036	0,0151	0- 4	0,9563

	80-84	20 673	0,173734742	3592	3 176	0,1536	75-79	0,5260
	85+	11 800	0,254100355	2998	2 650	0,2246	80+	0,3591
	KZN Total		LE=45,4	93169	82366	LE=48,4		
	Age category	Population in 2001	Derived m(x) values	Deaths	Adjusted		Survival ratios	
					Deaths	m(x)	Categories	Values
LIM	0	61 848	0,085874091	5311	4 695	0,0759	Birth	0,9159
	1-4	273 599	0,010264272	2808	2 482	0,0091	0- 4	0,9735

	80-84	17 848	0,155854418	2782	2 459	0,1378	75-79	0,5688
	85+	11 932	0,237456566	2833	2 505	0,2099	80+	0,3892
	LIM Total		LE=53,1	40481	35 787	LE=55,9		
MP	0	43 463	0,099171047	4310	3 810	0,0877	Birth	0,9017
	1-4	171 468	0,013264737	2274	2 010	0,0117	0- 4	0,9660

	80-84	7 503	0,164633858	1235	1 092	0,1455	75-79	0,5476
	85+	4 384	0,245634068	1077	952	0,2172	80+	0,3742
	MP Total		LE=49,4	26865	23 750	LE=52,3		
NC	0	12 576	0,066936442	842	744	0,0592	Birth	0,9355
	1-4	48 485	0,006619639	321	284	0,0059	0- 4	0,9828

	80-84	2 427	0,141625996	344	304	0,1253	75-79	0,6038
	85+	1 820	0,224177177	408	361	0,1982	80+	0,4140
	NC Total		LE=58,7	6201	5 482	LE=61,2		
NW	0	36 840	0,087281737	3215	2 842	0,0772	Birth	0,9144
	1-4	140 356	0,010564783	1483	1 311	0,0093	0- 4	0,9728

	80-84	7 284	0,156823615	1142	1 010	0,1386	75-79	0,5664
	85+	5 319	0,238359776	1268	1 121	0,2107	80+	0,3875
	NW Total		LE=52,7	22997	20331	LE=55,5		
WC	0	43 634	0,046253351	2018	1 784	0,0409	Birth	0,9564
	1-4	168 864	0,003477976	587	519	0,0031	0- 4	0,9909

	80-84	8 708	0,122492877	1067	943	0,1083	75-79	0,6526
	85+	6 439	0,206225574	1328	1 174	0,1823	80+	0,4489
	WC Total		LE=65,4	17183	15190	LE=67,6		
Total number of deaths (all provinces) = 333314								
RSA	0	496 043	0,077923398	38 653	RSA Total deaths = 294666			
	1-4	2 025 591	0,008644808	17 511				
				
	80-84	108 170	0,150167930	16 244				
	85+	66 710	0,232154254	15 487				
			RSA LE=55,4					

3.6 Provincial population estimates for South Africa

The format that explains the cohort-component method used to project the provincial populations is shown in Table 7 below. The projection is for the Eastern Cape female population. Please note that the same population was used in the discussion of mortality (Table 6) and migration (Table 5).

Table 7: Projection of the Eastern Cape female population (part 1)

Age	Population 2001	Survival ratio (Table 6)	Age specific fertility	Migration rates (per thousands of population) to:							
				FS (Table 5)	GT*	KZN	LIM	MP	NC	NW	WC
Births after 2001	426 668	0,9177		0,00194	0,00952	0,00567	0,00106	0,00154	0,00055	0,00393	0,01649
0-4	387 164	0,9745		0,00251	0,00895	0,00575	0,00118	0,00127	0,00069	0,00316	0,01854
5-9	446 561	0,9908		0,00241	0,00826	0,00570	0,00070	0,00121	0,00067	0,00197	0,01895
10-14	450 993	0,9878		0,00384	0,01833	0,01170	0,00131	0,00215	0,00099	0,00396	0,03849
15-19	403 541	0,9802	0,0609	0,00601	0,04179	0,02177	0,00226	0,00332	0,00102	0,00962	0,07114
20-24	305 412	0,9742	0,1380	0,00486	0,03634	0,01525	0,00232	0,00328	0,00104	0,01000	0,05298
25-29	253 482	0,9696	0,1644	0,00345	0,01678	0,00799	0,00192	0,00219	0,00067	0,00641	0,02520
30-34	199 671	0,9645	0,1431	0,00229	0,01090	0,00555	0,00121	0,00144	0,00057	0,00428	0,01579
35-39	182 789	0,9579	0,0994	0,00159	0,00745	0,00388	0,00084	0,00087	0,00045	0,00258	0,01107
40-44	182 212	0,9476	0,0436	0,00094	0,00455	0,00237	0,00054	0,00044	0,00041	0,00123	0,00701
45-49	153 021	0,9305	0,0162	0,00061	0,00258	0,00160	0,00028	0,00029	0,00022	0,00049	0,00449
50-54	127 907	0,9049		0,00036	0,00162	0,00101	0,00014	0,00018	0,00020	0,00032	0,00318
55-59	108 174	0,8693		0,00035	0,00128	0,00087	0,00014	0,00020	0,00011	0,00023	0,00264
60-64	119 473	0,8217		0,00027	0,00087	0,00052	0,00006	0,00014	0,00007	0,00012	0,00175
65-69	91 015	0,7580		0,00021	0,00057	0,00050	0,00007	0,00009	0,00008	0,00011	0,00125
70-74	61 401	0,6754		0,00018	0,00054	0,00023	0,00006	0,00009	0,00005	0,00009	0,00073
75-79	35 740	0,5717		0,00012	0,00033	0,00018	0,00004	0,00005	0,00003	0,00004	0,00052
80+	31 958	0,3913		0,00006	0,00022	0,00011	0,00003	0,00003	0,00003	0,00005	0,00036

* The calculations of the migration rates to the other provinces as well as the age specific fertility rates are not given in this document

The main steps in deriving provincial mid-year population estimates for South Africa are as follows.

3.6.1 Calculate the number of out-migrants (5 years and older)

Whereas a projection for a single region involves multiplying the population at the first time-point in each five-year age group by a survival rate to obtain the survivors to the next five-year age group at the second time point, a multi-regional projection involves a compound survival rate which specifies the probability of surviving and being in a particular region at the second time-point. A compound survival rate is the product of the survival rate and the out-migration rate(s) to each of the other provinces. The number of out-migrants from province A to each of the other provinces (B to I) is then defined as:

$$\begin{aligned} \text{OUT}_{t+5,x+5}^{AB} &= P_{t,x}^A * S_{t,x}^A * MR_{t,x}^{AB} \\ \text{OUT}_{t+5,x+5}^{AC} &= P_{t,x}^A * S_{t,x}^A * MR_{t,x}^{AC} \\ &\cdot \\ &\cdot \\ \text{OUT}_{t+5,x+5}^{AI} &= P_{t,x}^A * S_{t,x}^A * MR_{t,x}^{AI} \end{aligned}$$

Where:

$S_{t,x}^A$ is the survival ratio of province A, age group x, first projection period; $MR_{t,x}^{AB}$ is the migration rate of province A to province B, age group x, first projection period; $MR_{t,x}^{AC}$ is the migration rate of province A to province C, age group x, first projection period; and $MR_{t,x}^{AI}$ is the migration rate of province A to province I, age group x, first projection period. The migration rate is defined as the number of migrants per thousand of the population in a specific age group.

3.6.2 Calculate the number of survivors by province (5 years and older)

For survival in the same province, the compound rate is the survival rate times one minus the sum of the out-migration to the other provinces. That is, the survivors (those that have not died or migrated) for people in age group x+5 and period t+5 of province A are obtained by using the following formula:

$$\text{SUR}_{t+5,x+5}^A = P_{t,x}^A * S_{t,x}^A * (1 - MR_{t,x}^{AB} - MR_{t,x}^{AC} - MR_{t,x}^{AD} - \dots \dots \dots MR_{t,x}^{AI})$$

Where: $P_{t,x}^A$ is the population of province A, age group x, first time period; and the other symbols are defined as before. The number of survivors in each of the other provinces is calculated in the same way.

Applying the formulas in sections 3.6.1 and 3.6.2 and using the data in Table 7 will result in the number of out-migrants as set out in Table 8. The calculations in Tables 7 and 8 will have to be repeated for all the other female population in the other provinces (not shown). The same format, except for the fertility assumptions, is used for the male populations.

Table 8: Projection of the Eastern Cape female population (Part 2)

	Survivors in EC	Number of out migrants to:								In-migrants To EC*	Projected Population 2006
		FS	GT	KZN	LIM	MP	NC	NW	WC		
0-4	375 618	758	3 729	2 221	414	603	217	1 540	6 457	6 351	381 969
5-9	361 426	947	3 377	2 169	445	479	260	1 192	6 995	6 358	367 784
10-14	424 812	1 066	3 655	2 522	310	535	296	872	8 384	5 772	430 584
15-19	409 509	1 711	8 166	5 212	584	958	441	1 764	17 147	6 874	416 383
20-24	333 477	2 377	16 530	8 611	894	1 313	403	3 805	28 139	7 487	340 964
25-29	260 022	1 446	10 812	4 537	690	976	309	2 975	15 763	7 997	268 019
30-34	229 897	848	4 122	1 964	472	538	165	1 575	6 194	6 650	236 547
35-39	184 488	441	2 099	1 069	233	277	110	824	3 041	4 493	188 981
40-44	170 063	278	1 304	679	147	152	79	452	1 938	2 912	172 975
45-49	169 644	162	786	409	93	76	71	212	1 210	1 907	171 551
50-54	140 882	87	367	228	40	41	31	70	639	1 312	142 194
55-59	114 932	42	188	117	16	21	23	37	368	884	115 816
60-64	93 488	33	120	82	13	19	10	22	248	636	94 124
65-69	97 798	27	85	51	6	14	7	12	172	327	98 125
70-74	68 791	14	39	34	5	6	6	8	86	134	68 925
75-79	41 389	7	22	10	2	4	2	4	30	57	41 446
80+	32 900	3	10	5	1	1	1	2	16	27	32 927
Total	3 509 136	10 247	55 411	29 920	4 365	6 013	2 431	15 366	96 827		3 569 314

* To obtain the in-migrants to the EC, similar calculations were done for all the other provinces.

3.6.3 Calculate the number of in-migrants (5 years and older)

The number of in-migrants to province A (see second last column in Table 8) is obtained by adding the out-migrants from the other provinces (B to I) to province A, that is:

$$IN_{t+5,x+5}^A = OUT_{t+5,x+5}^{BA} + OUT_{t+5,x+5}^{CA} + OUT_{t+5,x+5}^{DA} + \dots + OUT_{t+5,x+5}^{IA}$$

3.6.4 Projected population (5 years and older)

The projected provincial population of A in each age group aged 5 years and older (see last column in Table 8) is simply the sum of the survivors in province A and the number of in-migrants to province A, namely:

$$P_{t+5,x+5}^A = SUR_{t+5,x+5}^A + IN_{t+5,x+5}^A$$

3.6.5 Calculate the number of births and survivors aged 0–4 years

Annual births are estimated by applying the age-specific birth rates assumed for each province to the number of women in each of the reproductive age groups. This step is done separately for 1996 and 2001. The results are averaged and then multiplied by five to obtain the total number of births in the specific province for the first five-year projection interval. The total number of births is multiplied by the assumed sex ratio at birth to obtain the number of male births. The projected 0–4 population (see first entry in the last column of Table 8) is calculated by applying the formula in sections 3.6.1 to 3.6.4.

This projection process can be repeated for further time intervals and the assumed levels of mortality, fertility and migration can be altered for each projection period, if desired.

7. District council projections

7.1 The age-sex structures of the base populations

The base age/sex structures of the district councils were determined through an iteration process and using the following datasets:

- The projected provincial populations by sex and five-year age groups;
- The district council and metro populations for Census 2001 by age and sex;
- First estimates of the district council totals by sex.

In this projection the first estimates were obtained by applying estimated birth, death and net migration data for the period 1996 to 2001 (from Census 2001) to the adjusted 1996 Census totals. This analysis provides an estimate of the relative size of the district councils and was done separately for males and females.

7.2 The migration trends between district councils/metros

The same method was used as described in section 3.3 for the provinces. The only difference is that the nine provinces are replaced with the 52 district councils and metros. One hundred and four tables (52x2) of the format of Table 7 will have to be constructed and 5304 (52x51x2) similar to Table 8.

To determine a usual and previous district council/metro for every person was more complicated than in the case of the provinces. We however managed to determine in 94,1% of the cases a previous district council / metro. More detail in this regard is given in Table 9 below.

Table 9: Result of migration calculations regarding previous district council/metros (2001 census)

	Number	Percentage
District Council/metro determined	42 161 155	94,1
No response	143 595	0,3
Place outside RSA	181 408	0,4
Can not identify District Council/metro	232 260	0,5
Invalid main place	23 185	0,1
Children born in 5 years before the census and who are not children of the head of the household	2 078 175	4,6
Total	44 819 778	100,0

7.3 Fertility estimation of district councils and metros

The following steps were used to obtain a set of age-specific fertility rates for each district council and each metro to be used in these cohort-component projections:

- For each district council and each metro a preliminary set of age-specific fertility rates were obtained. In this analysis the rates were taken from the fertility data of Census 2001 and adjusted by the Brass technique.
- Using the recorded births datasets from 1998–2008, the results obtained from the analyses in (a) were placed into perspective. Adjustments were made if necessary.
- The preliminary age-specific fertility rates were then applied to the appropriate female population aged 15 to 49 years to calculate the number of births. This was done for each district council and metro.

- (d) The total number of births generated from the district councils and metros were then compared with the total births from the provincial projection in which the district councils and metros fall (phase two). Proportional adjustments were made if necessary and adjusted TFRs calculated.
- (e) Using these adjusted TFRs and age-specific fertility rates as well as survival ratios, the number of births and the projected 0–4 aged population were obtained. The projected 0–4 year and 5–9 year populations were checked for consistency. Provision was made to adjust the TFR manually if inconsistencies were found.
- (f) The process (a) to (d) above was repeated if inconsistencies were found in (d).

7.4 Mortality estimation of district councils and metros

The following steps were used to obtain a set of survival ratios for each province to be used in the provincial cohort-component projections:

- (a) For each district council and metro a preliminary set of life expectancies at birth for males and females were obtained. In this analysis these rates were obtained from the mortality information in Census 2001. The crude death rate was used to determine the relative size of mortality. The actual level was calculated as described in (b) to (e) below.
- (b) Analyses of the causes of death datasets were done and the results were compared with the crude death rates obtained in (a). If necessary adjustments were made.
- (c) Separate Life Tables for males and females and for each district council / metro were then constructed from these preliminary set of life expectancies at birth (Far-East pattern of the UN used).
- (d) By using the $m(x)$ -values (age-specific mortality rates) in these life tables the number of deaths by age can then be calculated for both males and females in each district council and metro.
- (e) The total number of deaths calculated for each district council and metro were then compared with the total number of deaths generated in the province in which the district council / metro falls. This analysis was obviously done separately for males and females. Proportional adjustments were made if necessary.
- (f) The adjusted $m(x)$ values are then used to construct life tables. Life expectancies at birth as well as survival ratios by age can be read from the obtained life tables.

Conclusion

In October 2010, Stats SA for the first time made available estimates on the District Council level on its website. This might be seen as a Beta version and were based on the population figures in the 2010 mid-year release. District Council estimates based on the March 2011 boundaries and using estimates from the 2011 mid-year estimates will be available during September 2011. Users are invited to make use of the opportunity and to engage in a discussion of the results. This will enable Stats SA to make changes, especially regarding our migration assumptions on district council and metro levels. The migration data are based on information in Census 2001 regarding movements in the period 1996 to 2001 and as already indicated this data are becoming a little bit “old”. The Community Survey that was conducted in February 2007, however, shed more light on population numbers and migration patterns in the period after 2001.

REFERENCES

- HSRC, 2009. South African National HIV Prevalence, Incidence, Behaviour and Communication Survey, 2008: A Turning Tide among Teenagers?. HSRC Press, Pretoria.
- Moultrie T & Dorrington R. 2004. *Estimation of fertility from the 2001 South African Census data*. Centre for Actuarial Research, University of Cape Town.
- Statistics South Africa. 2008. Mid-year estimates 2008. (Statistical Release P0302).
- Stover J. 2003. *AIM version 4. A computer program for HIV/AIDS projections and examining the social and economic impacts of AIDS*. Spectrum system of Policy Models. The Futures Group International.
- United Nations. 1992. *Preparing Migration Data for Subnational Population Projections*. Department of International and Economic and Social Affairs. United Nations, New York.
- United Nations. 2002a. *HIV/AIDS and fertility in sub-Saharan Africa: A perspective of the research literature*. United Nations, New York.
- United Nations. 2002b. *Fertility levels and trends in countries with intermediate levels of fertility: A background paper for the Expert Group Meeting on Completing the Fertility Transition*. 11-14 March 2002. United Nations, New York.
- Willekens F & Rogers A. 1978. *Spatial Population Analysis: Methods and Computer Programs*. International Institute for Applied System Analysis. Research Report, RR 78-18. Laxenberg, Austria.

Willekens F, Por A, & Raquillet R. 1978. *Entropy, multiproportional, and quadratic techniques for inferring detailed migration patterns from aggregate data*. International Institute for Applied System Analysis. Working Paper, WP-79-88. Laxenberg, Austria.

World Health Organisation. 2001. *Prevention of mother-to-child transmission of HIV: Selection and use of Nevirapine*. Technical notes. World Health Organisation, Geneva, Switzerland.